

Possibly Useful Information

Constants & Conversions:

$$\begin{aligned}
 g &= 9.81 \text{ m/s}^2 & e &= 1.60 \times 10^{-19} \text{ C} & \epsilon_0 &= 8.85 \times 10^{-12} \frac{\text{C}^2}{\text{Nm}^2} \\
 k &= \frac{1}{4\pi\epsilon_0} = 8.99 \times 10^9 \frac{\text{Nm}^2}{\text{C}^2} & \mu_0 &= 4\pi \times 10^{-7} \frac{\text{T} \cdot \text{m}}{\text{A}} & c &= 3.0 \times 10^8 \frac{\text{m}}{\text{s}} \\
 1 \text{ eV} &= 1.602 \times 10^{-19} \text{ J} & 1 \text{ V} &= 1 \text{ J/C} = 1 \text{ Nm/C} & 1 \text{ H} &= 1 \text{ Tm}^2/\text{A} & 1 \text{ W} &= 1 \text{ J/s} \\
 1 \text{ A} &= 1 \frac{\text{C}}{\text{s}} & 1 \text{ T} &= 1 \frac{\text{N}}{\text{A} \cdot \text{m}} & 1 \text{ H} &= \frac{\text{T} \cdot \text{m}^2}{\text{A}} = 1 \Omega \cdot \text{s} & 1 \text{ F} &= 1 \frac{\text{C}}{\text{V}} = 1 \frac{\text{s}}{\Omega} \\
 m_p &= 1.67 \times 10^{-27} \text{ kg} & m_e &= 9.11 \times 10^{-31} \text{ kg} \\
 C &= 2\pi r & A &= \pi r^2 & A &= 4\pi r^2 & V &= (4/3)\pi r^3 & 180^\circ &\text{in } \Delta
 \end{aligned}$$

Current, Resistance & Circuits:

$$\begin{aligned}
 I &= \frac{dq}{dt} & I &= \int \vec{J} \cdot d\vec{A} & I &= JA & \vec{J} &= ne\vec{v}_d & \vec{E} &= \rho\vec{J} \\
 R &= \frac{V}{I} & \sigma &= \frac{1}{\rho} & R &= \frac{\rho L}{A} & \rho - \rho_0 &= \rho_0 \alpha (T - T_0) \\
 P &= IV = I^2 R = \frac{V^2}{R} & P &= \frac{\Delta E}{\Delta t} & \mathcal{E} &= \frac{dW}{dq} & U &= q\Delta V \\
 R_{eq} &= \sum_{j=1}^n R_j & \frac{1}{R_{eq}} &= \sum_{j=1}^n \frac{1}{R_j} & \Delta V_{loop} &= 0 & \sum I_{junc} &= 0 \\
 I &= \left(\frac{\mathcal{E}}{R} \right) e^{-t/RC} & V_C &= \mathcal{E} (1 - e^{-t/RC}) & q &= q_0 e^{-t/RC} & I &= - \left(\frac{q_0}{RC} \right) e^{-t/RC} & \tau_C &= RC
 \end{aligned}$$

Magnetic Fields:

$$\begin{aligned}
 \vec{F}_B &= q\vec{v} \times \vec{B} & F_B &= \frac{mv^2}{r} & \vec{F}_B &= I\vec{L} \times \vec{B} \\
 \mu &= NIA & \vec{\tau} &= \vec{\mu} \times \vec{B} & U(\theta) &= -\vec{\mu} \cdot \vec{B} \\
 d\vec{B} &= \frac{\mu_0}{4\pi} \frac{Id\vec{s} \times \hat{r}}{r^2} & \oint \vec{B} \cdot d\vec{s} &= \mu_0 I_{enc} & \Phi_B &= \int \vec{B} \cdot d\vec{A} \\
 B &= \frac{\mu_0 I}{2\pi r} & B &= \frac{\mu_0 I \phi}{4\pi R} & B &= \mu_0 nI & B &= \frac{\mu_0 IN}{2\pi r} & B &= \frac{\mu_0 IR^2}{2(R^2 + x^2)^{3/2}}
 \end{aligned}$$

Magnetic Induction:

$$\begin{aligned}
 \mathcal{E} &= - \frac{d\Phi_B}{dt} & \oint \vec{E} \cdot d\vec{s} &= - \frac{d\Phi_B}{dt} & L &= \frac{N\Phi_B}{I} & \mathcal{E}_L &= -L \frac{dI}{dt} \\
 L &= \mu_0 n^2 A \ell & L &= \frac{\mu_0 N^2 h}{2\pi} \ln \frac{b}{a} & I &= \frac{\mathcal{E}}{R} (1 - e^{-t/\tau_L}) & I &= I_0 e^{-t/\tau_L} & \tau_L &= \frac{L}{R} \\
 U_B &= \frac{1}{2} LI^2 & u_B &= \frac{B^2}{2\mu_0} & \oint \vec{B} \cdot d\vec{A} &= 0
 \end{aligned}$$

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LC Oscillations:

$$\omega^2 = \frac{1}{LC} \quad V = V_{\max} \sin(\omega t + \phi_V) \quad I = I_{\max} \sin(\omega t + \phi_I)$$

$$q = q_{\max} \cos(\omega t + \phi) \quad q = q_{\max} e^{-Rt/2L} \cos(\omega' t + \phi) \quad \omega' = \sqrt{\omega^2 - (R/2L)^2}$$

Equations from Exam 1:

Electric Force and Electric Fields:

$$\vec{F}_{12} = \frac{kq_1q_2}{r^2} \hat{r} \quad q = Ne \quad \vec{F} = q\vec{E} \quad \vec{E} = \frac{kq}{r^2} \hat{r}$$

$$\vec{E} = \sum_i \vec{E}_i = \sum_i \frac{kq_i}{r_i^2} \hat{r}_i \quad \vec{E} = \int d\vec{E} = \int \frac{k dq}{r^2} \hat{r}$$

$$\vec{p} = q\vec{d} \quad \vec{\tau} = \vec{p} \times \vec{E} \quad U = -\vec{p} \cdot \vec{E}$$

$$\Phi = \int \vec{E} \cdot d\vec{A} \quad \oint \vec{E} \cdot d\vec{A} = \frac{q_{\text{enc}}}{\epsilon_0}$$

$$E = \frac{q}{4\pi\epsilon_0 r^2} \quad E = \frac{\lambda}{2\pi\epsilon_0 r} \quad E = \frac{\sigma}{2\epsilon_0} \quad E_{\text{cond}} = \frac{\sigma}{\epsilon_0}$$

$$\lambda = \frac{Q}{L} = \frac{dq}{d\ell} \quad \sigma = \frac{Q}{A} = \frac{dq}{dA} \quad \rho = \frac{Q}{V} = \frac{dq}{dV}$$

Electric Fields and Potentials:

$$\Delta U = U_f - U_i = -W_{\text{field}} \quad U = \frac{kq_1q_2}{r} \quad V = \frac{kq}{r}$$

$$V = \sum_i V_i = \sum_i \frac{kq_i}{r_i} \quad V = \int dV = \int \frac{k dq}{r}$$

$$\Delta V = V_f - V_i = -\frac{W_{\text{field}}}{q} = -\int_i^f \vec{E} \cdot d\vec{s} \quad \vec{E} = -\nabla V = -\left(\frac{\partial V}{\partial x} \hat{i} + \frac{\partial V}{\partial y} \hat{j} + \frac{\partial V}{\partial z} \hat{k}\right)$$

Capacitance:

$$q = C\Delta V \quad C = \frac{\epsilon_0 A}{d} \quad C = 2\pi\epsilon_0 \frac{L}{\ln(b/a)} \quad C = 4\pi\epsilon_0 \frac{ab}{b-a}$$

$$C = 4\pi\epsilon_0 R \quad C_{\text{eq}} = \sum_{j=1}^n C_j \quad \frac{1}{C_{\text{eq}}} = \sum_{j=1}^n \frac{1}{C_j}$$

$$U = \frac{q^2}{2C} = \frac{1}{2} C (\Delta V)^2 \quad u = \frac{1}{2} \epsilon_0 E^2 \quad C = \kappa C_0 \quad \epsilon_0 \oint \kappa \vec{E} \cdot d\vec{A} = q$$